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## Final Exam Version A - DSC 80, Spring 2024

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**Instructions:**

- This exam consists of 14 questions. A total of 100 points are available.
- Questions marked with (M) will be used for your midterm exam redemption.
- Write name in the top right of each page in the space provided.
- Please write neatly in the provided answer boxes. We will not grade work that appears elsewhere.
- Completely fill in bubbles and square boxes.
  - A bubble means that you should only **select one choice**.
  - A square box means you should **select all that apply**.
- You may refer to two 8.5" × 11" sheets of notes of your own creation. No other resources or technology (including calculators) are permitted.
- Do not turn the page until instructed to do so.

Last name	
First name	
Student ID number	
UCSD email	
Name of the person to your left	
Name of the person to your right	
<i>All the work on this exam is my own.</i> <b>(please sign)</b>	

Name: \_\_\_\_\_

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Name: \_\_\_\_\_

**Question 1..... 6 points**

(M) Fill in Python code below so that the last line of each code snippet evaluates to each desired result, using the `df` and `survey` DataFrames described on Page 1 of the Reference Sheet. **You may not use for or while loops in any answer for this question.** For convenience, the first few rows of `df` (top) and `survey` (bottom) are displayed below; see your Reference Sheet for the full details.

	date	cost	q	state	name	cat	id
0	2023-01-03	20.99	1.0	VA	JIAFUEO Ziplock Bag Organizer, Bamboo Ziplock ...	FOOD_STORAGE_BAG	P2955
1	2023-01-03	23.84	1.0	VA	Briarwood Lane St Pat's Pickup St Patricks Day...	RUG	P2955
2	2023-01-25	12.63	1.0	VA	Pentatonix Deluxe Version	ABIS_MUSIC	P2955

	id	age	income	state	marijuana	diabetes
0	P0001	35 - 44 years	\$25,000 - \$49,999	Iowa	No	No
1	P0002	45 - 54 years	\$100,000 - \$149,999	Ohio	No	No
2	P0003	25 - 34 years	\$25,000 - \$49,999	Arkansas	No	Yes

(a) (2 points) Find the participant ID of the person who made the most recent purchase in the dataset.

```
df.sort_values(_____, ascending=True).iloc[_____, _____]
```

(b) (4 points) Create a DataFrame that compares the range of item costs for people with diabetes and people that don't have diabetes. The DataFrame should be indexed by the unique values in the `diabetes` column (Yes and No) and have one column: the range of item costs (max cost - min cost) for each group.

```
def f(x):  
    return _____
```

```
(df.merge(survey, on='id')  
.groupby(_____) [_____] )  
._____ (f)
```

**Question 2..... 2 points**

(a) (1 point) (M) What is the most likely missingness mechanism for the `state` column in `df`?

- Missing by design
- Missing completely at random
- Missing at random
- Not missing at random

(b) (1 point) (M) What is the most likely missingness mechanism for the `income` column in `survey`?

- Missing by design
- Missing completely at random
- Missing at random
- Not missing at random

Name: \_\_\_\_\_

**Question 3**..... *7 points*

(M) The code snippet below uses a for loop.

```
mystery = 0
for i in df['id'].unique():
    temp = df[df['id'] == i]
    if temp['q'].sum() > 100:
        mystery += 1
```

(a) (5 points) Rewrite the snippet without using any loops.

```
mystery = (df.groupby(_____)
._____(lambda x: _____)
[_____]._____())
```

(b) (2 points) Suppose you see the output below:

```
>>> df['id'].value_counts()
P2955    200
P3001    150
P3125    100
Name: id, Length: 3, dtype: int64
```

Fill in the blank in the sentence below with a single number.

The code without for loops runs approximately \_\_\_\_\_ times faster than the code with a for loop.

**Question 4**..... *10 points*

You want to use regular expressions to extract out the number of ounces from the 5 product names below.

Index	Product Name	Expected Output
0	Adult Dog Food 18-Count, 3.5 oz Pouches	3.5
1	Gardetto's Snack Mix, 1.75 Ounce	1.75
2	Colgate Whitening Toothpaste, 3 oz Tube	3
3	Adult Dog Food, 13.2 oz. Cans 24 Pack	13.2
4	Keratin Hair Spray 2!6 oz	6

The names are stored in a pandas Series called names. For each snippet below, select the indexes for all the product names that **will not** be matched correctly.

(a) (5 points) Snippet:

```
regex = r'([\d.]+) oz'
names.str.findall(regex)
```

0    1    2    3    4    All names will be matched correctly.

(b) (5 points) Snippet:

```
regex = r'(\d+?.\d+) oz|Ounce'
names.str.findall(regex)
```

0    1    2    3    4    All names will be matched correctly.

Name: \_\_\_\_\_

**Question 5**..... *4 points*

(M) Suppose you define a DataFrame `t` as follows:

```
t = (survey.merge(df, on='id', suffixes=('', '2'))
      .assign(is_ca=t['state'] == 'California',
              is_boot=t['cat'] == 'BOOT',
              is_tool=t['cat'] == 'TOOLS'))
```

The first few rows of `t` are shown below:

	id	age	income	state	...	cat	is_ca	is_boot	is_tool
0	P1852	18 - 24 years	\$75,000 - \$99,999	Maryland	...	COMPUTER	False	False	False
1	P2244	25 - 34 years	Less than \$25,000	North Carolina	...	WATER	False	False	False
2	P2244	25 - 34 years	Less than \$25,000	North Carolina	...	FRUIT_SNACK	False	False	False

For each pivot table below, state whether it is **possible** to observe Simpson's paradox without any extra information about the data.

(a) (2 points) Pivot table:

```
t.pivot_table(
    index='is_ca',
    columns='is_boot',
    values='cost',
    aggfunc='count',
)
```

- Yes    No    Need more information to determine

(b) (2 points) Pivot table:

```
t.pivot_table(
    index='is_ca',
    columns='is_tool',
    values='cost',
    aggfunc='mean',
)
```

- Yes    No    Need more information to determine

Name: \_\_\_\_\_

**Question 6**..... **9 points**

(M) For each hypothesis test below, select the **one** correct procedure to simulate a single sample under the null hypothesis, and select the **one** test statistic that can be used for the hypothesis test among the choices given. For convenience, the first few rows of `df` (top) and `survey` (bottom) are displayed below; see your Reference Sheet for the full details.

	date	cost	q	state	name	cat	id
0	2023-01-03	20.99	1.0	VA	JIAFUEO Ziplock Bag Organizer, Bamboo Ziplock ...	FOOD_STORAGE_BAG	P2955
1	2023-01-03	23.84	1.0	VA	Briarwood Lane St Pat's Pickup St Patricks Day...	RUG	P2955
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	id	age	income	state	marijuana	diabetes
0	P0001	35 - 44 years	\$25,000 - \$49,999	Iowa	No	No
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2	P0003	25 - 34 years	\$25,000 - \$49,999	Arkansas	No	Yes

- (a) (3 points) Null: Every purchase is equally likely to happen in all 50 states.  
Alternative: At least one state is more likely to have purchases than others.

Simulation procedure:

- `np.random.multinomial(len(df), [1/50] * 50)`
- `np.random.multinomial(len(survey), [1/50] * 50)`
- `np.random.multinomial(len(df), [1/2] * 2)`
- `np.random.permutation(df['state'])`

Test statistic:

- Difference in means
- Absolute difference in means
- Total variation distance
- K-S test statistic

- (b) (3 points) Null: The income distribution of people who smoke marijuana is the same as the income distribution for people who don't smoke marijuana.  
Alternative: The income distributions are different.

Simulation procedure:

- `np.random.multinomial(len(survey), [1/50] * 50)`
- `np.random.multinomial(len(survey), [1/2] * 2)`
- `np.random.permutation(survey['income'])`

Test statistic:

- Difference in means
- Absolute difference in means
- Total variation distance
- K-S test statistic

- (c) (3 points) Null: The distribution of prices for items with missing categories is the same as the distribution of prices for items with recorded categories.  
Alternative: Items with missing categories are more expensive than items with recorded categories.

Simulation procedure:

- `np.random.multinomial(len(df), [1/50] * 50)`
- `np.random.multinomial(len(df), [1/2] * 2)`
- `np.random.permutation(df['cost'])`

Test statistic:

- Difference in means
- Absolute difference in means
- Total variation distance
- K-S test statistic

**Question 7..... 6 points**

(M) Suppose that `df` doesn't have any missing data in the `cost` column. Sam accidentally loses values from the `cost` column and values are more likely to be missing for `states` with expensive purchases. Sam's data is stored in a DataFrame called `missing`.

To recover the missing values, Sam applies the imputation methods below to the `cost` column in `missing`, then recalculates the mean of the `cost` column. For each imputation method, choose whether the new mean will be lower (-), higher (+), exactly the same (=), or approximately the same ( $\approx$ ) as the original mean of the `cost` column in `df` (the data without any missing observations).

(a) (2 points) `missing['cost'].fillna(missing['cost'].mean())`

-  +  =   $\approx$

(b) (2 points)

```
def mystery(s):
    return s.fillna(s.mean())
missing.groupby('state')['cost'].transform(mystery).mean()
```

-  +  =   $\approx$

(c) (2 points)

```
def mystery2(s):
    s = s.copy()
    n = s.isna().sum()
    fill_values = np.random.choice(s.dropna(), n)
    s[s.isna()] = fill_values
    return s
```

```
missing.groupby('state')['cost'].transform(mystery2).mean()
```

-  +  =   $\approx$

Name: \_\_\_\_\_

**Question 8..... 8 points**

Suppose you are trying to scrape album names from a website. The website has an HTML table structured as follows:

```
<table><thead>
  <tr>
    <th>Name</th> <th>Price</th> <th>Number of Reviews</th>
  </tr></thead>
<tbody>
  <tr class="row">
    <td>Radical Optimism</td> <td>25</td> <td>10000</td>
  </tr>
  <tr class="row">
    <td>Hit Me Hard and Soft</td> <td>30</td> <td>12000</td>
  </tr>
  <tr class="row">
    <td>SOS</td> <td>18</td> <td>30000</td>
  </tr>
  <!-- 997 <tr> elements omitted -->
</tbody>
</table>
```

Notice that the `<tbody>` tag contains 1000 `<tr>` elements, but only the first three are shown above. Suppose that you've read the HTML table above into a BeautifulSoup object called `soup`. Fill in the code below so that the `albums` variable contains a list of all the album names with (strictly) more than 15,000 reviews.

```
albums = []
for tag in soup.find_all(___ (a) ___):
    reviews = int(___ (b) ___)
    if reviews > 15000:
        album = ___ (c) ___
        albums.append(album)
```

(a) (2 points) What should go in blank (a)?

(b) (3 points) What should go in blank (b)?

(c) (3 points) What should go in blank (c)?



Name: \_\_\_\_\_

**Question 9**..... **7 points**

You create a table called `gums` that only contains the chewing gum purchases of `df`, then you create a bag-of-words matrix called `bow` from the `name` column of `gums`. The `bow` matrix is stored as a DataFrame shown below:

	<b>pur</b>	<b>gum</b>	<b>...</b>	<b>paperboard</b>	<b>80</b>
<b>0</b>	0	1	...	0	1
<b>1</b>	0	1	...	1	1
<b>...</b>	<b>...</b>	<b>...</b>	<b>...</b>	<b>...</b>	<b>...</b>
<b>38</b>	0	0	...	0	0
<b>39</b>	0	0	...	0	1

You also have the following outputs:

```
>>> bow_df.sum(axis=0)    >>> bow_df.sum(axis=1)    >>> bow_df[0, 'pur']
pur                5          0    21                0
gum                41         1    22                0
sugar              2          2    22                >>> (bow_df['paperboard'] > 0).sum()
..                ..          ..                20
90                 4          37    22
paperboard        22         38    10                >>> bow_df['gum'].sum()
80                20         39    17                41
Length: 139          Length: 40
```

For each question below, write your answer as an unsimplified math expression (no need to simplify fractions or logarithms) in the space provided, or select "Need more information" if there is not enough information provided to answer the question.

(a) (2 points) What is the TF-IDF for the word `pur` in document 0?

Need more information

(b) (2 points) What is the TF-IDF for the word `gum` in document 0?

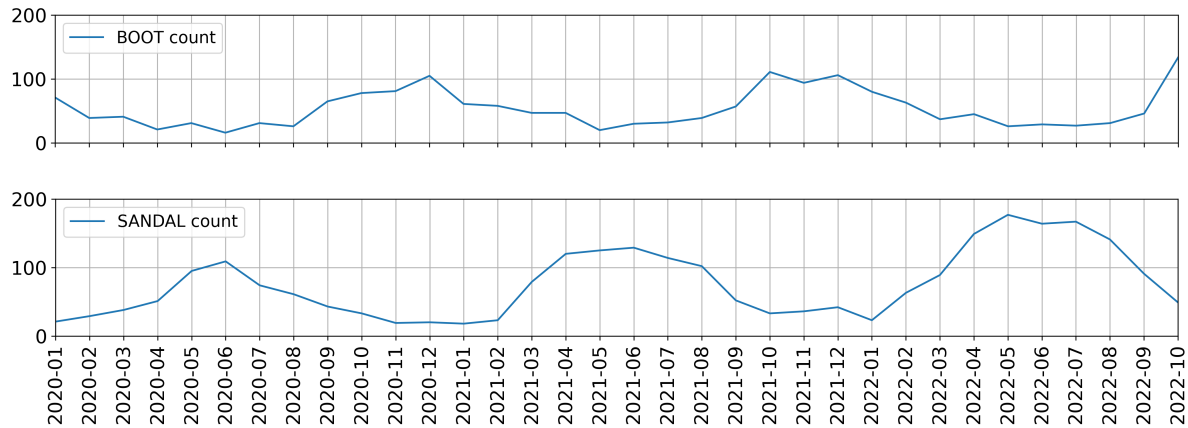
Need more information

(c) (3 points) What is the TF-IDF for the word `paperboard` in document 1?

Need more information

**Question 10** ..... **17 points**

The two plots below show the total number of boots (top) and sandals (bottom) purchased per month in the df table. Assume that there is one data point per month.



For each of the following regression models, use the visualizations shown above to select the value that is *closest* to the fitted model weights. If it is not possible to determine the model weight, select “Not enough info”. For the models below: the notation `boot` refers to the number of boots sold; `sandal` refers to the number of sandals sold; `summer=1` is a column with value 1 if the month is between March (03) and August (08), inclusive; and `winter=1` is a column with value 1 if the month is between September (09) and February (02), inclusive.

- (a) (2 points)  $\text{boot} = w_0$   
 $w_0$ :  0    50    100    Not enough info
  
- (b) (4 points)  $\text{boot} = w_0 + w_1 \cdot \text{sandal}$   
 $w_0$ :  -100    -1    0    1    100    Not enough info  
 $w_1$ :  -100    -1    1    100    Not enough info
  
- (c) (4 points)  $\text{boot} = w_0 + w_1 \cdot (\text{summer}=1)$   
 $w_0$ :  -100    -1    0    1    100    Not enough info  
 $w_1$ :  -80    -1    0    1    80    Not enough info
  
- (d) (4 points)  $\text{sandal} = w_0 + w_1 \cdot (\text{summer}=1)$   
 $w_0$ :  -20    -1    0    1    20    Not enough info  
 $w_1$ :  -80    -1    0    1    80    Not enough info
  
- (e) (3 points)  $\text{sandal} = w_0 + w_1 \cdot (\text{summer}=1) + w_2 \cdot (\text{winter}=1)$   
 $w_0$ :  -20    -1    0    1    20    Not enough info  
 $w_1$ :  -80    -1    0    1    80    Not enough info  
 $w_2$ :  -80    -1    0    1    80    Not enough info

Name: \_\_\_\_\_

**Question 11.....9 points**

Suppose you fit four different models to predict whether someone has an income greater than \$100,000 a year using their purchase history. You split the data into a training and test set and use 3-fold cross-validation. The table below shows all the calculated accuracies for each model (higher accuracy is better).

	train	fold 1	fold 2	fold 3	test
<b>Model A</b>	0.5	0.4	0.5	0.3	0.4
<b>Model B</b>	0.7	0.6	0.8	0.9	0.5
<b>Model C</b>	0.8	0.9	0.2	0.1	0.6
<b>Model D</b>	1.0	0.8	0.3	0.5	0.3

- (a) (2 points) Which model has the lowest model bias?  
 Model A    Model B    Model C    Model D
- (b) (2 points) Which model most severely underfits the data?  
 Model A    Model B    Model C    Model D
- (c) (2 points) Which model most severely overfits the data?  
 Model A    Model B    Model C    Model D
- (d) (3 points) Which model should you pick overall?  
 Model A    Model B    Model C    Model D

Name: \_\_\_\_\_

**Question 12..... 8 points**

Suppose you fit a decision tree to the training set below, using the features  $x_0$  and  $x_1$  to predict the outcome  $y$ .

$x_0$	$x_1$	$y$
0	0	0
0	1	0
0	2	1
1	0	0
1	1	1
2	0	1
2	1	1
3	0	1

Write the first four splitting rules that are created by the decision tree when fitting this training set (using weighted entropy). Assume that the tree is constructed in a depth-first order. If two candidate splits have the same weighted entropy, choose the one that splits on  $x_0$ .

- (a) The first splitting rule is: \_\_\_(i)\_\_\_  $\leq$  \_\_\_(ii)\_\_\_
- i. (1 point) What goes in blank (i)?  
  $x_0$      $x_1$
  - ii. (1 point) What goes in blank (ii)?  
 0    1    2    3
- (b) The second splitting rule is: \_\_\_(i)\_\_\_  $\leq$  \_\_\_(ii)\_\_\_
- i. (1 point) What goes in blank (i)?  
  $x_0$      $x_1$
  - ii. (1 point) What goes in blank (ii)?  
 0    1    2    3
- (c) The third splitting rule is: \_\_\_(i)\_\_\_  $\leq$  \_\_\_(ii)\_\_\_
- i. (1 point) What goes in blank (i)?  
  $x_0$      $x_1$
  - ii. (1 point) What goes in blank (ii)?  
 0    1    2    3
- (d) The fourth splitting rule is: \_\_\_(i)\_\_\_  $\leq$  \_\_\_(ii)\_\_\_
- i. (1 point) What goes in blank (i)?  
  $x_0$      $x_1$
  - ii. (1 point) What goes in blank (ii)?  
 0    1    2    3

Name: \_\_\_\_\_

**Question 13**..... *7 points*

Suppose you fit a logistic regression classifier. The classifier's predictions on a test set of 5 points are shown below, along with the actual labels.

Predicted Probability	Actual $y$
0.3	1
0.4	0
0.6	1
0.7	1
0.3	0

Recall that for logistic regression, we must also choose a threshold  $\tau$  to convert the predicted probabilities to predicted labels. For this question, assume that  $0 < \tau < 1$ . For this question, precision is undefined when the classifier doesn't make any positive predictions (since  $\frac{0}{0}$  is undefined). For each question, show your work and draw a box around your final answer in the space provided. Each of your final answers should be a single number.

- (a) (2 points) What is the **lowest** possible precision for any threshold  $\tau$ ?

- (b) (2 points) What is the **lowest** possible recall for any threshold  $\tau$ ?

- (c) (3 points) What is the **highest** possible recall if the classifier achieves a precision of 1?

Name: \_\_\_\_\_

**Question 14.....0 points**  
Optional: Draw a Picture About UCSD Data Science (or use this page for scratch work)